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## Reservoir Screening for $\mathbf{C O}_{2}$ Sequestration

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## Table of Contents

Introduction ..... 2
Definitions and Units ..... 3
Properties of $\mathrm{CO}_{2}$ ..... 4
$\mathrm{CO}_{2}$ Sequestration in Aquifers ..... 13
Natural Gas and Natural Gas Reservoirs ..... 19
$\mathrm{CO}_{2}$ Sequestration in Abandoned Gas Reservoirs ..... 41
$\mathrm{CO}_{2}$ Sequestration in Abandoned Gas Reservoirs - Limited Information ..... 47
Conclusion ..... 51
References ..... 52

## Reservoir Screening for $\mathrm{CO}_{2}$ Sequestration

## Introduction

Due to the concern over the amount of carbon dioxide $\left(\mathrm{CO}_{2}\right)$ being emitted into the atmosphere by industry, enterprises have been created to capture and store (known as sequestration) $\mathrm{CO}_{2}$ in subsurface reservoirs. This is typically referred to as CCS, or Carbon Capture and Storage. Any potential reservoir of interest must be screened for viability and $\mathrm{CO}_{2}$ storage volume. The purpose of this course is to educate one on how to estimate the volume of $\mathrm{CO}_{2}$ that can be sequestered in particular reservoirs. This is a necessary step to determine whether a reservoir, or reservoirs are capable of sequestering a given amount of $\mathrm{CO}_{2}$.

The course will not discuss the subjects of injection rates, well placement, or timing of injection. It is assumed, because of the enormity of such projects that once a reservoir is chosen it will be modeled to determine well placement and injection rates.

There are three types of reservoirs that are potential candidates for the sequestration of $\mathrm{CO}_{2}$. Reservoirs are defined as rock formations which contain pores or pore space where fluids can exist. The reservoirs available for $\mathrm{CO}_{2}$ sequestration are:

- Aquifers
- Abandoned natural gas reservoirs
- Oil reservoirs

This course will discuss storage in aquifers and abandoned natural gas reservoirs. The injection of $\mathrm{CO}_{2}$ into oil reservoirs is a tertiary recovery process. Additional oil is recovered as $\mathrm{CO}_{2}$ is absorbed by the oil (known as miscibility) and reduces the surface tension and viscosity of the oil. Due to the complexity of the process and the fact that there are texts and courses covering this subject, we will eliminate oil reservoirs from discussion in this course.

An aquifer is a reservoir where the pore space is entirely filled with water. In particular, salt-water aquifers are the ones of choice because they are not used for drinking water. $\mathrm{CO}_{2}$ has the ability to dissolve in water (i.e., club soda) and therefore has the potential to be stored there. It should be mentioned that the ability of water to store $\mathrm{CO}_{2}$ decreases with salt content.

Some of the best candidates for $\mathrm{CO}_{2}$ sequestration are abandoned natural gas reservoirs. The pore space in these reservoirs contain a percentage of water (known as water saturation) and a percentage of space taken up by gas known as hydrocarbon pore volume (HCPV). This allows $\mathrm{CO}_{2}$ to be compressed into the HCPV and also some of the $\mathrm{CO}_{2}$ to dissolve into the water in the reservoir.

## Definitions and Units

This course will involve the use of several terms, abbreviated symbols, and various units of measurement. The tables below define certain terms, abbreviated symbols and their associated units of measurement.

| Terms, Definitions, Units, and Symbols |  |  |  |
| :---: | :---: | :---: | :---: |
| Term | Definition | Units | Symbol |
| Abandonment Pressure | The pressure at which a reservoir ceases production. | psia | $\mathrm{P}_{\mathrm{ab}}$ |
| $\mathrm{CO}_{2}$ Sequestration | The storage of CO 2 in subsurface reservoirs |  |  |
| $\mathrm{CO}_{2}$ Solubiity in Water | The amount of CO 2 that can be disolved in water. | lb |  |
| Cubic Feet | A measurement of volume. | $\mathrm{ft}^{3}$ or cf |  |
| Cumulative Gas | The gas produced from initial conditions to the current date. | MMscf | G |
| Density | The mass of a substance per unit volume. | $\mathrm{lb} / \mathrm{ft}^{3}$ | r |
| Gas Deviation Factor | A factor used to adust the Ideal Gas Law for the molecular interactions of hydrocarbon gases. | No Units | z |
| Gas Formation Volume Factor | The volume of 1 standard cubic foot of gas at reservoir conditions. | $\mathrm{ft}^{3} / \mathrm{scf}$ | $\mathrm{B}_{\mathrm{g}}$ |
| Hydrocarbon Pore Volume | The volume of the reservoir capable of containing fluids minus water. | $\mathrm{ft}^{3}$ | HCPV |
| Initial Pressure | The pressure in a reservoir at initial conditions. | psia | $\mathrm{P}_{\mathrm{i}}$ |
| Million Cubic Feet | A measurement of volume. | MMcf |  |
| Natural Gas | A natural gaseous substance primarily composed of hydrocarbons. |  |  |
| Original gas-in-place | The gas volume contained in the reservoir at initial conditions. | MMscf | OGIP |
| Pore Volume | The volume of the reservoir capable of containing fluids. | $\mathrm{ft}^{3}$ | PV |
| Porosity | The non-solid portion of a rock capable of holding fluids. | $\begin{gathered} \text { \% or } \\ \text { decimal } \end{gathered}$ | Ф |
| Pound | A measurement of weight or mass. | lb |  |
| Reservoir | A rock unit containing pore space capable of holding fluids. |  |  |
| Reservoir Area | The areal extent of a reservoir. | acres |  |
| Reservoir Height | The vertical height of a reservoir. | ft acre-ft or |  |
| Reservoir Volume | The reservoir area multiplied by the reservoir height. | $\mathrm{ft}^{3}$ | $V_{r}$ |
| Residual Gas | The gas remaining in the reservoir at abandonment. | MMscf | $\mathrm{G}_{\text {res }}$ |
| Sequestration Pressure | The pressure at which CO 2 will be stored in a reservoir. | psia | $\mathrm{P}_{\mathrm{s}}$ |
| Standard Conditions | The state of a fluid at standard pressure and temperature. |  |  |
| Standard Cubic Feet | A measurement of volume at standard conditions. The pressure at which fluids are measured. Each state has its own | scf |  |
| Standard Pressure | under the tab "State Pressure Bases" in the accompanying Excel workbook. | psia |  |
| Standard Temperature | The temperature at which fluids are measured. The standard temperature is $60^{\circ} \mathrm{F}$. | ${ }^{\circ} \mathrm{F}$ |  |
| Thousand Cubic Feet | A measurement of volume. | Mcf |  |
| Water Saturation | The portion of the porosity filled with water. | $\begin{gathered} \text { \% or } \\ \text { decimal } \end{gathered}$ | Sw |

There is sometimes confusion using the terms for cubic feet as $\mathrm{ft}^{3}$ and cf . These unit symbols have identical meanings. Reservoir volumes are large and the units used are typically thousands or millions of cubic feet. The symbols for these, respectively are Mcf and MMcf rather than Mft ${ }^{3}$ and $\mathrm{MMft}^{3}$. When referring to thousand and millions of standard cubic feet the symbols Mscf and MMscf are used.

## Properties of $\mathbf{C O}_{2}$

When one thinks of $\mathrm{CO}_{2}$, one normally thinks of it as a gas at atmospheric conditions. One may also be familiar with a solid form of $\mathrm{CO}_{2}$ known as "dry ice" used as a coolant for packaged goods. Dry ice is so named because it does not melt, but immediately turns to $\mathrm{CO}_{2}$ gas. This is known as sublimation. One never observes $\mathrm{CO}_{2}$ as a liquid because it doesn't exist at atmospheric conditions.

Shown below is a phase diagram of $\mathrm{CO}_{2}$. A phase diagram shows the various phases of a substance (solid, liquid, gas) at various temperatures and pressures.


As we will soon see, $\mathrm{CO}_{2}$ will exist as a supercritical fluid under most subsurface reservoir conditions.

The table below lists some of the important properties of $\mathrm{CO}_{2}$.

| Properties of Carbon Dioxide |  |
| :--- | :---: |
| Chemical Formula | $\mathrm{CO}_{2}$ |
| Molecular Weight (g/mol) | 44.01 |
| Critical Pressure (psia) | 1,070 |
| Critical Temperature $\left({ }^{\circ} \mathrm{F}\right)$ | 87 |
| Phase at Standard Conditions | Gas |
| Specific Gravity at Standard Conditions | 1.52 |
| Density at Standard Conditions (lb/scf) | 0.115 |

There are two properties of $\mathrm{CO}_{2}$ that are most important when calculating the amount of $\mathrm{CO}_{2}$ that can be sequestered in a reservoir. These are $\mathrm{CO}_{2}$ density and $\mathrm{CO}_{2}$ solubility in water.

As with other substances, the density of $\mathrm{CO}_{2}$ changes as its phase changes. Density is defined as mass per unit of volume. For this course we will use pounds per cubic foot $\left(\mathrm{lb} / \mathrm{ft}^{3}\right) . \mathrm{CO}_{2}$ density can be found in several sources. The one we will use for this course is a website from the National Institute of Standards and Technology of the US Department of Commerce. The website is:

## Thermophysical Properties of Fluid Systems (nist.gov)

Opening the page gives this menu:


From the drop-down box I have chosen "carbon dioxide" and the following units for each of the items:

- Temperature - Fahrenheit
- Pressure - psia
- Density - lbm/ft ${ }^{3}$
- Energy - Bru/lbm
- Velocity - ft/s
- Viscosity - cp
- Surface tension - lb/in
- Data type - Isothermal properties
- Standard state convention - Default for fluid

Clicking on the "Press to Continue" button, the following screen comes up:

## Isothermal Properties for Carbon dioxide

```
This option will supply data on a constant temperature curve over the specified pressure range. Values should not extend ex
1. Enter temperature in selected units:
```



```
2. Enter pressure range and increment in selected units:
```



```
* The maximum pressure limit is the lowest of the following values:
- 116030.2 psia
- The pressure at which a density of \(73.568 \mathrm{lbm} / \mathrm{ft} 3\) is reached.
3. Check here if you want to use the intereactive display (requires JavaScript and HTML 5 canvas capable browser) \(\square\)
4. Number of digits to be displayed in tables (does not effect accuracy of computations): \(5 \mathbf{V}\)
Press for Data
```

For a given reservoir of interest, you will know the reservoir pressure and temperature. For this example, I chose a temperature of $120^{\circ} \mathrm{F}$, low pressure of 100 psia , a high pressure of $2,500 \mathrm{psia}$ and a pressure increment of 100 psia. Clicking on the "Press for Data" button will give the chart shown on the following page.

| Fluid Data <br> Isothermal D | Data for $T$ | $=120.00 \mathrm{~F}$ |  |  |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Temperature (F) | Pressure (psia) | Density (lbm/ttz) | Volume (fta/bm) | Internal Energy (Btu/lbm) | Enthalpy (Btu/lbm) | Entropy (Btu/lbm*) | Cv (Btu/lmmR) | Cp (Btu/lbm*R) ${ }^{\text {s }}$ | Sound Spd. (tt/s) | Joule-Thomson (F/psia) ${ }^{\text {V }}$ | Viscosity (cp) ${ }^{\text {T }}$ | Therm. Cond. (w/m*K) | Phase |
| 120.00 | 100.00 | - 0.72704 | 1.3754 | 198.98 | 224.45 | 0.58094 | 0.16532 | 0.21657 | 901.09 | 0.11181 | 0.016125 | 0.018809 | vapor |
| 120.00 | 200.00 | 1.4969 | 0.66804 | 197.23 | 221.97 | 0.54659 | 0.16847 | 0.22696 | 886.98 | 0.11189 | 0.016230 | 0.019246 | vapor |
| 120.00 | 300.00 | 2.3162 | 0.43174 | 195.38 | 219.37 | 0.52504 | 0.17183 | 0.23902 | 872.53 | 0.11186 | 0.016359 | 0.019753 | por |
| 120.00 | 400.00 | 3.1931 | - 0.31317 | 193.42 | 216.62 | 0.50858 | 0.17543 | 0.25321 | 857.70 | 0.11171 | 0.016517 | 0.020349 | vapor |
| 120.00 | 500.00 | 4.1383 | 0.24165 | 191.33 | 213.70 | 0.49477 | 0.17932 | 0.27019 | 842.47 | 0.11139 | 0.016712 | 0.021057 | vapor |
| 120.00 | 60.00 | 5.1655 | 0.19359 | 189.08 | 210.59 | 0.48249 | 0.18357 | 0.29089 | 826.81 | 0.11085 | 0.016953 | 0.021911 | vapor |
| 120.00 | 700.00 | - 6.2934 | 0.15890 | 186.64 | 207.24 | 0.47110 | 0.18825 | 0.31675 | 810.70 | 0.11002 | 0.017254 | 0.022962 | vapor |
| 120.00 | 800.00 | 7 7.5479 | 0.13249 | 183.97 | 203.60 | 0.46019 | 0.19347 | 0.34998 | 794.13 | 0.10877 | 0.017633 | 0.024284 | vapor |
| 120.00 | 900.00 | 8.9663 | 0.11153 | 181.01 | 199.60 | 0.44940 | 0.19940 | 0.39429 | 777.12 | 0.10697 | 0.018122 | 0.025993 | vapor |
| 120.00 | 1000.0 | - 10.605 | 0.094294 | 177.66 | 195.12 | 0.43840 | 0.20624 | 0.45615 | 759.75 | 0.10437 | 0.018768 | 0.028272 | vapor |
| 120.00 | 1100.0 | - 12.555 | 0.079649 | 173.78 | 190.00 | 0.42680 | 0.21431 | 0.54782 | 742.21 | 0.10063 | 0.019654 | 0.031423 | vapor |
| 120.00 | 1100.0 | - 12.555 | 0.079649 | 173.78 | 190.00 | 0.42680 | 0.21431 | 0.54782 | 742.21 | 0.10063 | 0.019654 | 0.031423 | supercritical |
| 120.00 | 1100.0 | - 12.555 | 0.079649 | 173.78 | 190.00 | 0.42680 | 0.21431 | 0.54782 | 742.21 | 0.10063 | 0.019654 | 0.03142 | supercritical |
| 120.00 | 1200.0 | 14.973 | 0.066788 | 169.14 | 183.98 | 0.41408 | 0.22392 | 0.69407 | 725.14 | 0.095152 | 0.020939 | 0.035950 | supercritical |
| 120.00 | 1300.0 | 18.141 | 0.055124 | 163.35 | 176.62 | 0.39943 | 0.23502 | 0.94397 | 710.71 | 0.086964 | 0.022952 | 0.042620 | supercritical |
| 120.00 | 1400.0 | 22.497 | 0.044451 | 155.95 | 167.47 | 0.38206 | 0.24553 | 1.3399 | 706.55 | 0.074774 | 0.026372 | 0.051796 | supercritical |
| 120.00 | 1500.0 | - 28.018 | 0.035691 | 147.40 | 157.31 | 0.36326 | 0.24887 | 1.6234 | 733.94 | 0.059183 | 0.031899 | 0.060462 | supercritical |
| 120.00 | 1600.0 | 32.998 | 0.030305 | 140.28 | 149.25 | 0.34832 | 0.24379 | 1.4316 | 803.85 | 0.045127 | 0.038162 | 0.064556 | supercritical |
| 120.00 | 1700.0 | 36.493 | 0.027402 | 135.44 | 144.06 | 0.33844 | 0.23791 | 1.1703 | 889.30 | 0.035429 | 0.043384 | 0.066902 | supercritical |
| 120.00 | 1800.0 | 38.948 | 0.025676 | 132.05 | 140.61 | 0.33164 | 0.23355 | 0.99594 | 970.15 | 0.029015 | 0.047511 | 0.069123 | supercritical |
| 120.00 | 1900.0 | - 40.795 | 0.024513 | 129.48 | 138.11 | 0.32652 | 0.23045 | 0.88394 | 1043.3 | 0.024543 | 0.050896 | 0.071299 | supercritical |
| 120.00 | 2000.0 | 42.268 | 0.023659 | 127.42 | 136.18 | 0.32243 | 0.22814 | 0.80700 | 1109.3 | 0.021240 | 0.053780 | 0.073356 | supercritical |
| 120.00 | 2100.0 | 43.489 | 0.022994 | 125.69 | 134.63 | 0.31901 | 0.22635 | 0.75090 | 1169.5 | 0.018688 | 0.056310 | 0.075277 | supercritical |
| 120.00 | 2200.0 | 44.534 | 0.022455 | 124.20 | 133.35 | 0.31607 | 0.22490 | 0.70818 | 1224.9 | 0.016649 | 0.058578 | 0.077070 | supercritical |
| 120.00 | 2300.0 | - 45.446 | 0.022004 | 122.88 | 132.26 | 0.31348 | 0.22371 | 0.67454 | 1276.2 | 0.014976 | 0.060642 | 0.078747 | supercritical |
| 120.00 | 2400.0 | 46.258 | 0.021618 | 121.71 | 131.31 | 0.31116 | 0.22271 | 0.64735 | 1324.2 | 0.013575 | 0.062547 | 0.080323 | supercritical |
| 120.00 | 2500.0 | \| 46.988 | -0.021282 | 120.64 | 130.49 | 0.30905 | 0.22186 | 0.62488 | 1369.2 | 0.012381 | 0.064322 | 0.081811 | supercritical |

Auxiliary Data
Reference States, IIR Convention

```
EnthalpyH=200 kJ/kg at 0}\mp@subsup{0}{}{\circ}\textrm{C}\mathrm{ for saturated liquid.
```

Entropy $s=1 \mathrm{~J} / \mathrm{g}^{*} \mathrm{~K}$ at $0^{\circ} \mathrm{C}$ for saturated liquid.

Additional fluid properties
Critical temperature ( $\mathrm{T}_{\mathrm{C}}$ ) $\quad 87.7608 \mathrm{~F}$

| Critical pressure $\left(\mathrm{P}_{\mathrm{c}}\right)$ | 1070.0 psis |
| :--- | ---: |
| Critical density $\left(\mathrm{D}_{\mathrm{d}}\right)$ | $29.1913 \mathrm{lbm} / \mathrm{AB}$ |


| Critical density ( $\mathbf{D C}_{\text {d }}$ ) | $29.1913 \mathrm{lbm} / \mathrm{tt3}$ |
| :--- | ---: |
| Acentric factor | 0.22394 |


| Acentric factor | 0.22394 |
| :--- | ---: | ---: |
| Normal boiling point | -109.24 F |


| Normal boiling point | -109.24 F |
| :--- | ---: |
| Dipole moment | 0.0 Debye |

Although the chart is small here in the text, the temperature is listed in column 1, the pressure in column 2 , and the density in column 3 . The column at the far right lists the phase of $\mathrm{CO}_{2}$ as it exists at each temperature and pressure.

The example below will allow you to use the website to find the density of $\mathrm{CO}_{2}$.

## Example Problem:

Find the density of $\mathrm{CO}_{2}$ at a temperature of $125^{\circ} \mathrm{F}$ and a pressure of $2,700 \mathrm{psia}$.

## Answer:

Using the NIST website, the density is $47.164 \mathrm{lbm} / \mathrm{ft}^{3}$ as shown in the table below:

$$
\text { Isothermal Data for } \mathrm{T}=125.00 \mathrm{~F}
$$

| Temperature (F) | Pressure (psia) | Density (lbm/ft3) |
| ---: | ---: | ---: |
| 125.00 | 2500.0 | 45.765 |
| 125.00 | 2600.0 | 46.496 |
| 125.00 | 2700.0 | 47.164 |

Data for $\mathrm{CO}_{2}$ solubility in water is extremely difficult to find. Even when found, almost all solubilities are for $\mathrm{CO}_{2}$ dissolved in fresh water. Additionally, the units are typically moles of $\mathrm{CO}_{2}$ per liter and require conversions to field units. A reference that contains a graph of solubility data is a publication by the Interstate Oil Compact Commission in 1983 titled Improved Oil Recovery. Shown below is a graph of $\mathrm{CO}_{2}$ solubility in distilled water at various temperatures and pressures.


From Improved Oil Recovery, Interstate Oil Compact Commission, 1983
Note that the solubility (listed on the y-axis) is given in $\mathrm{kg} \mathrm{CO}_{2}$ per 100 kg of $\mathrm{H}_{2} \mathrm{O}$. This is the same as $\mathrm{lb} \mathrm{CO}_{2}$ per 100 lb of $\mathrm{H}_{2} \mathrm{O}$. Also notice that the pressure is given in atmospheres and the temperature in ${ }^{\circ} \mathrm{C}$. A copy of this chart is in the workbook under the tab labeled " $\mathrm{CO}_{2}$ Solubility in Water Chart".

It will be necessary to convert pressure from psia to bars and temperature from ${ }^{\circ} \mathrm{F}$ to ${ }^{\circ} \mathrm{C}$ to use this chart. The equations below can be used for the conversion:

$$
\begin{gathered}
T_{o C}=\frac{\left(T_{o F}-32\right)}{1.8} \\
P_{b a r}=\frac{P_{p s i a}}{14.696}
\end{gathered}
$$

where,

$$
\begin{aligned}
& \mathrm{To}_{\mathrm{C}}=\text { temperature in }{ }^{\circ} \mathrm{C} \\
& \mathrm{To}_{\mathrm{F}}=\text { temperature in }{ }^{\circ} \mathrm{F} \\
& \mathrm{P}_{\text {bar }}=\text { pressure in bars } \\
& \mathrm{P}_{\text {psia }}=\text { pressure in psia }
\end{aligned}
$$

To understand the use of this graph, perform the following example.

## Example Problem:

Find the solubility of $\mathrm{CO}_{2}$ in water at a reservoir temperature of $122^{\circ} \mathrm{F}$ and pressure of 2,400 psia.

## Answer:

The first thing to do is to convert the reservoir temperature and pressure to units of the solubility graph. This is done as:

$$
\begin{gathered}
T_{o C}=\frac{\left(T_{o F}-32\right)}{1.8}=\frac{(122-32)}{1.8}=50 \mathrm{C} \\
P_{b a r}=\frac{P_{p s i a}}{14.504}=\frac{2,400}{14.696}=163 \mathrm{~atm}
\end{gathered}
$$

Entering the graph with the above values gives $5.5 \mathrm{lbm} \mathrm{CO}_{2}$ per $100 \mathrm{lbm}_{2} \mathrm{O}$ as shown below.


As mentioned in the introduction, $\mathrm{CO}_{2}$ solubility decreases with an increase in salinity. If an aquifer is being considered for $\mathrm{CO}_{2}$ sequestration, it is recommended that laboratory tests be done on a water sample to determine $\mathrm{CO}_{2}$ solubility. The graph on the following page (different units than the graph above) shows the effects of $10 \%$ salinity compared to distilled water. At $1,000 \mathrm{psi}$ the difference is a $40 \%$ loss in solubility at $75^{\circ} \mathrm{F}$ and a $25 \%$ reduction at $122^{\circ} \mathrm{F}$.

For all calculations in this course, we will use $\mathrm{CO}_{2}$ solubility data for distilled water.


From Improved Oil Recovery, Interstate Oil Compact Commission, 1983

## $\mathrm{CO}_{2}$ Sequestration in Aquifers

As mentioned above, $\mathrm{CO}_{2}$ can be sequestered in salt-water aquifers. Aquifers exist predominantly at hydrostatic pressure. Hydrostatic pressure is the pressure created by the height of water above the reservoir. For pure water (no salt), the hydrostatic pressure at a given depth can be calculated as:

$$
P=0.433 * H
$$

where,
$\mathrm{P}=$ reservoir pressure in psia
$\mathrm{H}=$ vertical depth from the surface to the reservoir in feet

Salt will increase the weight of water and also the pressure at any given depth. The graph below shows the relationship between water salinity, temperature, and pressure. Sea water contains about $35,000 \mathrm{ppm}$ salt and has a density of $63.96 \mathrm{lbm} / \mathrm{ft}^{3}(1.025 \mathrm{~g} / \mathrm{cc})$, which is a pressure gradient of $0.444 \mathrm{psi} / \mathrm{ft}$ of depth. For any aquifer of interest, the pressure at depth will most likely be known.


From Gearhart Owens, 1978

It will be assumed throughout this course that the sequestration pressure (the pressure under which $\mathrm{CO}_{2}$ will be stored in the reservoir) will not exceed the original pressures of either an aquifer or abandoned natural gas reservoir. The reason for this is the fact that the original fluids in the reservoir did not leak at original conditions. This is good evidence that $\mathrm{CO}_{2}$ will likely not leak when the reservoir is maintained at its original pressure.

Since aquifers are at or close to the original pressure when $\mathrm{CO}_{2}$ injection is commenced, the injection pressure must be closely monitored to prevent injecting above the fracture pressure. The fracture pressure is the pressure at which a hydraulic fracture is created in the reservoir. Most $\mathrm{CO}_{2}$ injection wells will likely be hydraulically fractured to allow for higher injection rates, so the fracture pressure will be known. Hydraulic fracture treatments will be designed such that no fractures leave the reservoir where they could create leaks above or below.

In an aquifer, the pore space is totally filled with water. The water is essentially a warehouse where $\mathrm{CO}_{2}$ will be stored. The diagrams below illustrate the pore space in the reservoir before and after $\mathrm{CO}_{2}$ sequestration.


The estimation of how much $\mathrm{CO}_{2}$ can be sequestered in an aquifer will follow these steps:

1) Determine the reservoir area, height, porosity, reservoir pressure, reservoir temperature, standard pressure and standard temperature. (This course will not go into detail on how to find or calculate these parameters, but they will be provided in examples and quiz questions).
2) Calculate the volume and weight of water in the reservoir
3) Estimate the solubility of $\mathrm{CO}_{2}$ in water at reservoir (sequestration) pressure and temperature.
4) Calculate how many pounds of $\mathrm{CO}_{2}$ that can be sequestered.
5) Calculate the volume of $\mathrm{CO}_{2}$ that can be sequestered in standard cubic feet.

As can be seen from the steps listed above, the estimation of how much $\mathrm{CO}_{2}$ that can be sequestered in an aquifer is fairly straight forward and is accomplished in just a few steps.

Step 5 is a conversion of $\mathrm{CO}_{2}$ sequestered to standard conditions. This is necessary since the $\mathrm{CO}_{2}$ being sequestered is produced and measured at atmospheric conditions. It also provides a standardized way of measuring $\mathrm{CO}_{2}$ volumes. The density of $\mathrm{CO}_{2}$ at standard conditions of $60^{\circ} \mathrm{F}$ and 14.65 psia is $0.115 \mathrm{lb} / \mathrm{ft}^{3}\left(\rho C O 2_{s t d}\right)$. The density of water at standard conditions is $62.4 \mathrm{lb} / \mathrm{ft}^{3}$.

Since water entirely fills the porosity of the reservoir, the volume of water in the aquifer is simply the pore volume of the reservoir. The pore volume can be calculated by the following equation:

$$
P V=0.04356 * A * h * \emptyset
$$

where,
$\mathrm{PV}=$ pore volume of reservoir in MMcf
$\mathrm{A}=$ reservoir area in acres
$\mathrm{H}=$ reservoir height in feet
$\emptyset=$ reservoir porosity as a decimal

The Excel workbook has a tab labeled "Sequestration in Aquifer" which can be used to estimate $\mathrm{CO}_{2}$ sequestration in aquifers. The spreadsheet can be used to solve any of the examples for aquifer sequestration in the text and the quiz. The spreadsheet has 50 rows for use when screening reservoirs for a $\mathrm{CO}_{2}$ sequestration project. Data is entered into the highlighted cells.

The example below will demonstrate how to estimate $\mathrm{CO}_{2}$ sequestration in an aquifer. This example is listed on Row 4 on the spreadsheet.

## Example Problem:

Estimate how much $\mathrm{CO}_{2}$ can be sequestered in an aquifer with the following properties. Express the answer in both pounds of $\mathrm{CO}_{2}$ and standard cubic feet of $\mathrm{CO}_{2}$ that can be sequestered.

Reservoir depth $=5,400 \mathrm{ft} \quad$ Reservoir area $=3,200$ acres $\quad$ Reservoir height $=50 \mathrm{ft}$
Reservoir porosity $=24.1 \% \quad$ Reservoir temp $=118^{\circ} \mathrm{F} \quad$ Reservoir pressure $=2,350 \mathrm{psia}$
Standard pressure $=14.65 \mathrm{psia} \quad$ Standard temp $=60^{\circ} \mathrm{F}$

## Answer:

Step 1) This is just the given data.

Step 2) Since the pore space of the reservoir is totally filled with water, the volume of water is simply the pore volume of the reservoir. The pore space of the reservoir is calculated from the formula below.

$$
P V=0.04356 * A * h * \emptyset
$$

where,
$\mathrm{PV}=$ pore volume of reservoir in MMcf
$\mathrm{A}=$ reservoir area in acres
$\mathrm{H}=$ reservoir height in feet
$\emptyset=$ reservoir porosity as a decimal

For this reservoir, the pore volume, or water volume is:

$$
P V=0.04356 * 3,200 * 50 * 0.241=1679.7 M M c f
$$

The weight of water in pounds is simply the volume multiplied by the water density of $62.4 \mathrm{lb} / \mathrm{ft}^{3}$ as follows:

$$
W=P V * \rho_{w}
$$

where,

$$
\begin{aligned}
& \mathrm{W}=\text { weight of water in million } \mathrm{lb} \\
& \mathrm{PV}=\text { pore volume in } \mathrm{MMcf} \\
& \rho_{w}=\text { density of water in } \mathrm{lb} / \mathrm{ft}^{3}
\end{aligned}
$$

So, the amount of water in the aquifer, expressed in millions of pounds is:

$$
W=P V * \rho_{w}=1679.7 * 62.4=104,811 \text { million } l b
$$

Step 3) Calculate the pressure in bars and the temperature in ${ }^{\circ} \mathrm{C}$, find water solubility from the chart.

$$
\begin{gathered}
T_{o C}=\frac{\left(T_{o F}-32\right)}{1.8}=\frac{(118-32)}{1.8}=48 \mathrm{C} \\
P_{b a r}=\frac{P_{p s i a}}{14.504}=\frac{2,350}{14.696}=160 \mathrm{~atm}
\end{gathered}
$$



The solubility is $5.7 \mathrm{lb} \mathrm{CO}_{2} / 100 \mathrm{lb}_{2} \mathrm{O}$.

Step 4) Calculate the lb of $\mathrm{CO}_{2}$ that can be sequestered in the aquifer. This will be the $\mathrm{CO}_{2}$ solubility multiplied by the amount of water in the reservoir as:

Sequestered $\mathrm{CO}_{2}=$ Water Mass $x \mathrm{CO}_{2}$ Solubility $=104,811 * \frac{5.7}{100}=5,974$ million lb

Step 5) Calculating the standard cubic feet of $\mathrm{CO}_{2}$ that can be sequestered is done by dividing the pounds of $\mathrm{CO}_{2}$ sequestered in the aquifer by the density of $\mathrm{CO}_{2}$ at standard conditions. The density of $\mathrm{CO}_{2}$ at standard conditions is $0.115 \mathrm{lb} / \mathrm{ft}^{3}$. Here is the calculation:

Sequestered CO2 at Std Conditions $=\frac{\text { Sequestered } \mathrm{CO}_{2} \text { in } \mathrm{lbs}}{\rho \mathrm{CO} 2_{\text {std }}}=\frac{5,974}{0.115}=51,948 \mathrm{MMscf}$
This problem has been input into the Excel workbook under the tab "Sequestration in Aquifer" on row 4.

## Natural Gas and Natural Gas Reservoirs

Before one can estimate how much $\mathrm{CO}_{2}$ can be sequestered in an abandoned natural gas reservoir, one must understand how natural gas and natural gas reservoirs behave. The following sections will discuss the ideal gas law, natural gas properties, how the gas deviation factor is determined and the gas formation volume factor is calculated.

## Ideal Gas Law

In order to understand gas properties, one must understand how gases behave. Gas molecules, unlike the other phases of matter - liquids and solids, are not bound together by intermolecular and viscous forces. As such, gases completely fill whatever container in which they reside. This property is very important and can be used to determine how gases behave under the effects of pressure, temperature, and volume.

The Ideal Gas Law is an equation of state that relates pressure, temperature, and volume. This equation is the results of combining Boyle's law, Charles' law, Avogadro's law, and Gay-Lussac's law. Shown below is the Ideal Gas Law equation of state:

$$
P V=n R T
$$

where,

```
\(P=\) pressure (psia - pounds per square inch absolute)
\(V=\) volume (scf - standard cubic feet)
\(T=\) temperature ( \({ }^{\circ} \mathrm{R}\) - degrees Rankine)
\(n=\) number of moles of gas (moles)
\(R=\) ideal gas constant ( 10.73 scf-psia/mole- \({ }^{\circ} \mathrm{R}\) )
```

The purpose of R, the ideal gas constant is to convert to consistent units. Depending on the units used, R will change. It should always be remembered that when dealing with gases, temperature is always in absolute units (i.e., Kelvin or Rankine). In the USA, we use units of Rankine (Fahrenheit plus 459.67 degrees).

Based on the Ideal Gas Law, one can derive a very important relationship. If a gas is composed of different types of molecules (i.e., nitrogen, oxygen, etc.), the volume percentage of each gas is equal to the molar percentage of that gas. This can be shown as follows:

Let $V$ be the total gas volume and N be the total number of moles. The Ideal Gas Law equation is then:

$$
P V=N R T
$$

Let $v$ be the volume of a single gas component and n be the moles of that component. The Ideal Gas Law for that component is then:

$$
P v=n R T
$$

Taking a ratio of the individual gas component to the total gas gives the following:

$$
\frac{P v}{P V}=\frac{n R T}{N R T}
$$

Since $P, R$, and $T$ are all equal, this equation can be simplified as:

$$
\frac{v}{V}=\frac{n}{N}
$$

This clearly shows that the ratio of an individual component to the total volume is the same as the number of moles of a component to the total number of moles of gas. This is very important because gas samples are analyzed in the laboratory and the results presented as mole percentages, which in effect are volume percentages.

This equation of state works well under normal ranges of pressure and temperature when the interaction between molecules is relatively small. In the case of hydrocarbon gases, however, the molecular interactions are not small and must be taken into account. For that purpose, the Ideal Gas Law is modified to account for these interactions. Shown below is the Ideal Gas Law equation modified for hydrocarbon gases:

$$
P V=n R T z
$$

where,

$$
z=\text { gas deviation factor }
$$

This course will discuss how to determine $z$ based on the reduced pressure and temperatures. The value for $z$ does depend on the constituents that make up the natural gas. Specifically, the value of z depends on the gas specific gravity and the reduced pressure and reduced temperature. The reduced pressure is the measured pressure divided by the critical pressure and the reduced temperature is the measured temperature divided by the critical temperature. The determination of the critical pressure and temperature will be discussed in a later section of this course. However, shown below are the equations for the reduced pressure and temperature.

$$
\begin{aligned}
& P r=P / P c \\
& T r=T / T c
\end{aligned}
$$

where,

$$
\begin{aligned}
& P r=\text { reduced pressure } \\
& P=\text { measured pressure }(\mathrm{psia}) \\
& P c=\text { critical pressure }(\mathrm{psia}) \\
& T r=\text { reduced temperature } \\
& T=\text { measured temperature }\left({ }^{\circ} \mathrm{R}\right) \\
& T c=\text { critical temperature }\left({ }^{\circ} \mathrm{R}\right)
\end{aligned}
$$

## Example Problem:

How many moles of gas are there in the container given the following data:

Container volume $=2 \mathrm{scf}$
Temperature $=80^{\circ} \mathrm{F}$
Pressure $=500 \mathrm{psia}$

## Answer:

The first thing to do is calculate the temperatures in absolute temperature degrees, so the temperature is:

$$
\mathrm{T}=80+459.67=539.67^{\circ} \mathrm{R}
$$

Rearrange the Ideal Gas Law equation to solve for " $n$ " as shown below:

$$
n=\frac{P V}{R T}=\frac{(500) *(2)}{(10.73) *(539.67)}=0.17 \text { moles }
$$

## What is Natural Gas

Most of us think of natural gas as something we use in our homes for heating or cooking. It is true that we tend to call gas delivered to our homes as "natural gas", but in reality, it is a nearly single component called "methane" that is derived from natural gas. So, what is natural gas and what is it composed of?

Webster's Dictionary defines natural gas as
"gas issuing from the earth's crust through natural openings or bored wells, especially a combustible mixture of methane and other hydrocarbons used chiefly as a fuel and raw material"

Natural gas is created in the earth's crust by the decay and reduction of organic material. As organic material is deposited on the earth's surface and subsequently buried, it is subjected to increased pressure and temperature. As this process continues, the organic material is reduced to petroleum. Depending on the composition of the original organic matter, the temperature, and pressure, the petroleum is either gaseous or liquid. As this petroleum forms, it begins to seep and being lighter than water, begins to move toward the earth's surface. This seeping petroleum moves along faults or through porous rocks and either makes it to the surface or is trapped along the way. There are various ways petroleum can be trapped, but most commonly with some type of seal like an impervious rock layer that prevents its further upward movement. The trapped petroleum exists in porous rocks known as reservoirs. Natural gas can exist in reservoirs as a gas or can be liberated from oil as it is produced. Natural gas can also exist in coal seams and is referred to as coalbed methane or coal seam gas. In the case of gas existing in coal seams, the coal is both the source rock and reservoir and the gas is actually attached to the surface of the coal.

Although there are gases emanating from the earth that do not contain hydrocarbons (i.e., nitrogen and carbon dioxide), the discussions in this course will be concerned only with hydrocarbon natural gases. Unlike non-hydrocarbon gases, hydrocarbon gases behave quite differently to pressure and temperature. With the exception of very high pressures and temperatures, non-hydrocarbon gases closely follow the Ideal Gas Law. The Ideal Gas Law is an equation of state that relates pressure, temperature and volume. Due to the interaction of hydrocarbon molecules, hydrocarbon gases deviate from the Ideal Gas Law. By analyzing the composition of natural gas, one can adjust the Ideal Gas Law to account for these interactions and properly calculate the relationship between pressure, temperature and volume.

## Components of Natural Gas

The most common hydrocarbon constituents of natural gas are known as alkanes or paraffins. An alkane is a molecule composed of carbon and hydrogen with single bonds between the atoms and
forming a chain-like structure. The simplest alkane is methane, which consists of a single carbon atom connected to four hydrogen atoms. Alkanes are named by the number of carbon atoms that make up the molecule. After methane, the next molecule containing two carbon atoms is called ethane. An alkane containing three carbon atoms is propane. Shown below are diagrams of the first four alkanes.

| Methane | Ethane | Propane | Butane |
| :---: | :---: | :---: | :---: |
|  |  |  |  |
| \| | \| | $1 \quad 1$ |  |
| H | H H | $\mathrm{H} \quad \mathrm{H}$ H | $\mathrm{H} \quad \mathrm{H} \quad \mathrm{H} \quad \mathrm{H}$ |

The first thing to notice is that there is a relationship between the number of hydrogen atoms and the number of carbon atoms. If n is the number of carbon atoms, then the number of hydrogen atoms is $2 \mathrm{n}+2$. Since there is a direct relationship between the carbon and hydrogen atoms that comprise alkane molecules, there is also a direct relationship between the molecular weight and heating content of the alkanes.

The molecular weight of carbon is approximately 12 pounds per pound-mole and the molecular weight of hydrogen is approximately 1 pound per pound-mole. Using the formula for the relationship between the number of carbon and hydrogen atoms gives an increase of 14 pounds per pound-mole for each increment in alkanes.

Hydrocarbons create energy by reacting with oxygen (i.e., burning or combustion). If one combines a hydrocarbon with oxygen, the result is carbon dioxide $\left(\mathrm{CO}_{2}\right)$, water $\left(\mathrm{H}_{2} \mathrm{O}\right)$, and heat. The amount of heat is directly proportional to the amount of carbon, hydrogen, and oxygen consumed in the process. Shown below are the equations for combustion for the first four alkanes.

| Methane | $\mathrm{CH}_{4}+2 \mathrm{O}_{2}=\mathrm{CO}_{2}+2 \mathrm{H}_{2} \mathrm{O}+$ Heat |
| :--- | :---: |
| Ethane | $2 \mathrm{C}_{2} \mathrm{H}_{6}+7 \mathrm{O}_{2}=4 \mathrm{CO}_{2}+6 \mathrm{H}_{2} \mathrm{O}+$ Heat |
| Propane | $\mathrm{C}_{3} \mathrm{H}_{8}+5 \mathrm{O}_{2}=3 \mathrm{CO}_{2}+4 \mathrm{H}_{2} \mathrm{O}+$ Heat |
| Butane | $2 \mathrm{C}_{4} \mathrm{H}_{10}+13 \mathrm{O}_{2}=8 \mathrm{CO}_{2}+10 \mathrm{H}_{2} \mathrm{O}+$ Heat |

## Example Problem:

a) How many hydrogen atoms are in a molecule of octane (8 carbons atoms)?
b) What is the estimated molecular weight?

## Answer:

a) Using the equation that hydrogen atoms are $2 \mathrm{n}+2$ carbon atoms:
$2 \times 8+2=18$ hydrogen atoms in octane
b) The estimated molecular weight is 12 times the number of carbon atoms plus 1 times the number of hydrogen atoms as:

Estimated molecular weight of octane $=12 \times 8+1 \times 18=114$ pound per pound-mole

Besides the major alkane hydrocarbons, there are other constituents of natural gas that occur. The most common of these are:

```
Air
Nitrogen \(\left(\mathrm{N}_{2}\right)\)
Oxygen ( \(\mathrm{O}_{2}\) )
Carbon Dioxide \(\left(\mathrm{CO}_{2}\right)\)
Hydrogen Sulfide \(\left(\mathrm{H}_{2} \mathrm{~S}\right)\)
Hydrogen \(\left(\mathrm{H}_{2}\right)\)
Argon (Ar)
Helium (He)
```

When computing properties of natural gas, these constituents must be taken into account as they affect the overall properties of the gas. As a rule, most of these constituents occur in minor amounts. The exception to this rule are carbon dioxide $\left(\mathrm{CO}_{2}\right)$ and nitrogen $\left(\mathrm{N}_{2}\right)$ which can sometimes occur in large amounts. Although some gas contracts allow for small amounts of nonhydrocarbons in the gas stream, prior to sale or use for commercial purposes, the major portion of these constituents must be removed. In gases containing hydrogen sulfide $\left(\mathrm{H}_{2} \mathrm{~S}\right)$, this constituent is extremely toxic and must always be removed prior to transmission or sale.

Table 1 shown on the next page lists the most common constituents of natural gas along with their molecular formula, molecular weight, critical pressure, and critical temperature. Occasionally, a natural gas contains other gases such as benzene or toluene. If these are present, their properties can be added to the table and used to calculate overall properties of the gas. The footnote on Table 1 gives the source of the gas property data and can be referenced for additional constituents.

| Component | Table 1 <br> Common Constituents of Natual Gases |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
|  | Molecular Formula | ${ }^{1,2}$ Molecular Weight | ${ }^{1,2}$ Critical <br> Pressure (psia) | ${ }^{1,2,3}$ Critical Temperature $\left({ }^{\circ} \mathrm{R}\right)$ |
| Methane | $\mathrm{CH}_{4}$ | 16.042 | 667.00 | 343.01 |
| Ethane | $\mathrm{C}_{2} \mathrm{H}_{6}$ | 30.069 | 706.60 | 549.59 |
| Propane | $\mathrm{C}_{3} \mathrm{H}_{8}$ | 44.096 | 615.50 | 665.59 |
| Iso-Butane | $\mathrm{C}_{4} \mathrm{H}_{10}$ | 58.122 | 527.90 | 734.08 |
| N-Butane | $\mathrm{C}_{4} \mathrm{H}_{10}$ | 58.122 | 550.90 | 765.22 |
| Iso-Pentane | $\mathrm{C}_{5} \mathrm{H}_{12}$ | 72.149 | 490.40 | 828.67 |
| N-Pentane | $\mathrm{C}_{5} \mathrm{H}_{12}$ | 72.149 | 488.80 | 845.47 |
| Hexane | $\mathrm{C}_{6} \mathrm{H}_{14}$ | 86.175 | 436.90 | 913.47 |
| Heptane | $\mathrm{C}_{7} \mathrm{H}_{16}$ | 100.202 | 396.80 | 972.57 |
| Octane | $\mathrm{C}_{8} \mathrm{H}_{18}$ | 114.229 | 360.70 | 1,023.87 |
| Nonane | $\mathrm{C}_{9} \mathrm{H}_{20}$ | 128.255 | 330.70 | 1,070.47 |
| Decane | $\mathrm{C}_{10} \mathrm{H}_{22}$ | 142.282 | 304.60 | 1,111.87 |
| Air |  | 28.959 | 551.90 | 238.70 |
| Nitrogen | $\mathrm{N}_{2}$ | 28.014 | 492.50 | 227.14 |
| Oxygen | $\mathrm{O}_{2}$ | 31.999 | 731.40 | 278.24 |
| Carbon Dioxide | $\mathrm{CO}_{2}$ | 44.010 | 1,070.00 | 547.45 |
| Hydrogen Sulfide | $\mathrm{H}_{2} \mathrm{~S}$ | 34.082 | 1,306.50 | 672.48 |
| Hydrogen | $\mathrm{H}_{2}$ | 2.016 | 190.70 | 59.77 |
| Argon | Ar | 39.948 | 705.32 | 271.24 |
| Helium | He | 4.003 | 33.00 | 9.35 |
| Notes: <br> 1 - From Gas Proces <br> 2 - From NIST Chem <br> 3 - Degrees Rankine | uppliers Assoc ebBook, SRD rees Fahrenhe | n Engineering Da https://webbook.n 459.67 | Book, Twelfth Ed ov/chemistry/flu | $\text { n, } 2004$ |

## Calculation of Natural Gas Properties from Gas Composition

The composition of a natural gas is made by analyzing a sample of the gas. The sample can be taken directly form the reservoir using a special device or can be taken at the surface from the production facilities. Once the sample is taken it is sent to a laboratory where measurements of the components and their proportion of the total gas are made.

The amount of each component of the gas sample is reported as "Mole $\%$ " which is the percentage of the number of molecules of the component divided by the total number of gas molecules. For a gas, the Mole \% is the same as the volume percent.

Shown below in Table 2 is an example of a gas sample.

| Table 2 <br> Example Gas Sample |  |
| :---: | :---: |
| Component | Measured Mole \% |
| Methane | 79.28 |
| Ethane | 3.55 |
| Propane | 3.43 |
| I-C4 | 1.80 |
| $\mathrm{N}-\mathrm{C} 4$ | 1.54 |
| I-C5 | 1.66 |
| N-C5 | 1.30 |
| C6 | 1.92 |
| C7 | 0.88 |
| C8 | 0.75 |
| C9 | 0.00 |
| C10 | 0.00 |
| O2 | 0.00 |
| N2 | 2.44 |
| CO 2 | 1.30 |
| H2S | 0.00 |
| Ar | 0.15 |
| Total | 100.00 |

Notice that many of the components are simply listed as the number of carbon atoms in the molecule. This is common practice in some labs. It is fortunate that for this gas sample the total of the constituents add up to 100 percent. In some cases, the total is not $100 \%$ and must be adjusted so the total is equal to 100 percent. Due to the methods used and the percision of the instruments making the measurements, the totals do not always add to 100 percent. In those cases, an adjustment to the percentage of each component must be made. Table 3 shows a gas sample where the components do not add up to 100 percent and the method used to correct the tabel values.

| Table 3Example Gas Sample Adjustment |  |  |
| :---: | :---: | :---: |
| Component | Measured Mole \% | Adjusted Mole \% |
| Methane | 78.20 | 78.61 |
| Ethane | 3.66 | 3.68 |
| Propane | 3.40 | 3.42 |
| I-C4 | 1.84 | 1.85 |
| N-C4 | 1.62 | 1.63 |
| I-C5 | 1.65 | 1.66 |
| N-C5 | 1.22 | 1.23 |
| C6 | 1.88 | 1.89 |
| C7 | 0.91 | 0.91 |
| C8 | 0.82 | 0.82 |
| C9 | 0.25 | 0.25 |
| C10 | 0.14 | 0.14 |
| O 2 | 0.00 | 0.00 |
| N2 | 2.44 | 2.45 |
| CO 2 | 1.30 | 1.31 |
| H2S | 0.00 | 0.00 |
| Ar | 0.15 | 0.15 |
| Total | 99.48 | 100.00 |
| Notes: <br> Adjusted Mole\% = Measured Mole \% / Total Measured Mole \% |  |  |

The adjusted mole percentages are just the measured mole percentages divided by the total of the measured mole percentages. When the total of the measured mole $\%$ is 98 percent or greater, this method can be used with fair accuracy. If the sum is less than 98 percent, the accuracy of this method decreases and might warrant an new gas sample.

Calculating the gas properties of the sampled gas is done by combining the results of the gas sample with the properties shown in Table 1. For the purpose of showing how to calculate gas properties of a gas sample, we will use the gas sample shown in Table 2. Table 4 on the next page combines the mole percentages of the gas sample in Table 2 and the properties of each component from Table 1 into a single table.

| Component | Table 4Gas Composition from Table 2 and Gas Properties from Table 1 |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  | Molecular Formula | Mole Fraction (\%) | Molecular Weight | Critical Pressure (psia) | Critical Temperature ( ${ }^{\circ} \mathrm{R}$ ) |
| Methane | $\mathrm{CH}_{4}$ | 79.28 | 16.042 | 667.00 | 343.01 |
| Ethane | $\mathrm{C}_{2} \mathrm{H}_{6}$ | 3.55 | 30.069 | 706.60 | 549.59 |
| Propane | $\mathrm{C}_{3} \mathrm{H}_{8}$ | 3.43 | 44.096 | 615.50 | 665.59 |
| Iso-Butane | $\mathrm{C}_{4} \mathrm{H}_{10}$ | 1.80 | 58.122 | 527.90 | 734.08 |
| N-Butane | $\mathrm{C}_{4} \mathrm{H}_{10}$ | 1.54 | 58.122 | 550.90 | 765.22 |
| Iso-Pentane | $\mathrm{C}_{5} \mathrm{H}_{12}$ | 1.66 | 72.149 | 490.40 | 828.67 |
| N-Pentane | $\mathrm{C}_{5} \mathrm{H}_{12}$ | 1.30 | 72.149 | 488.80 | 845.47 |
| Hexane | $\mathrm{C}_{6} \mathrm{H}_{14}$ | 1.92 | 86.175 | 436.90 | 913.47 |
| Heptane | $\mathrm{C}_{7} \mathrm{H}_{16}$ | 0.88 | 100.202 | 396.80 | 972.57 |
| Octane | $\mathrm{C}_{8} \mathrm{H}_{18}$ | 0.75 | 114.229 | 360.70 | 1,023.87 |
| Nonane | $\mathrm{C}_{9} \mathrm{H}_{20}$ | 0.00 | 128.255 | 330.70 | 1,070.47 |
| Decane | $\mathrm{C}_{10} \mathrm{H}_{22}$ | 0.00 | 142.282 | 304.60 | 1,111.87 |
| Air |  | 0.00 | 28.959 | 551.90 | 238.70 |
| Nitrogen | $\mathrm{N}_{2}$ | 2.44 | 28.014 | 492.50 | 227.14 |
| Oxygen | $\mathrm{O}_{2}$ | 0.00 | 31.999 | 731.40 | 278.24 |
| Carbon Dioxide | $\mathrm{CO}_{2}$ | 1.30 | 44.010 | 1,070.00 | 547.45 |
| Hydrogen Sulfide | $\mathrm{H}_{2} \mathrm{~S}$ | 0.00 | 34.082 | 1,306.50 | 672.48 |
| Hydrogen | $\mathrm{H}_{2}$ | 0.00 | 2.016 | 190.70 | 59.77 |
| Argon | Ar | 0.15 | 39.948 | 705.32 | 271.24 |
| Helium | He | 0.00 | 4.003 | 33.00 | 9.35 |
| Total |  | 100.00 |  |  |  |

To determine the properties of the gas sample, we will now add some columns to Table 4 so we can calculate the mole percentage weighted properties of each component. Table 5 shows the additional columns where the weighted values are tabulated and accumulated. To calculate the mole weighted value of each property, multiply the value for that property by the mole percentage for the given component. This table can be created manually, or it can be created using a spreadsheet program.

In this example, the mole percentage for ethane is $3.55 \%$. The value for the critical pressure of ethane is 706.6 psia. Multiplying 706.6 psia by $3.55 \%$ give a mole weighted value of 25 psia as shown in mole weighted critical pressure column for ethane. Once we have calculated the mole weighted values for each component in the gas sample, the values are summed to arrive at the properties for the gas sample.

| Component | Molecular Formula | Table 5Calculation of Mole Fraction Weighted Properties |  |  |  | Mole Fraction Weighted |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | Mole Fraction (\%) | Molecular Weight | Critical Pressure (psia) | Critical Temperature ( ${ }^{\circ} \mathrm{R}$ ) |  |  |  |
|  |  |  |  |  |  | Molecular Weight | Critical Pressure (psia) | Critical Temperature $\left({ }^{\circ} R\right)$ |
| Methane | $\mathrm{CH}_{4}$ | 79.28 | 16.042 | 667.00 | 343.01 | 12.72 | 529 | 272 |
| Ethane | $\mathrm{C}_{2} \mathrm{H}_{6}$ | 3.55 | 30.069 | 706.60 | 549.59 | 1.07 | 25 | 20 |
| Propane | $\mathrm{C}_{3} \mathrm{H}_{8}$ | 3.43 | 44.096 | 615.50 | 665.59 | 1.51 | 21 | 23 |
| Iso-Butane | $\mathrm{C}_{4} \mathrm{H}_{10}$ | 1.80 | 58.122 | 527.90 | 734.08 | 1.05 | 10 | 13 |
| N-Butane | $\mathrm{C}_{4} \mathrm{H}_{10}$ | 1.54 | 58.122 | 550.90 | 765.22 | 0.90 | 8 | 12 |
| Iso-Pentane | $\mathrm{C}_{5} \mathrm{H}_{12}$ | 1.66 | 72.149 | 490.40 | 828.67 | 1.20 | 8 | 14 |
| N-Pentane | $\mathrm{C}_{5} \mathrm{H}_{12}$ | 1.30 | 72.149 | 488.80 | 845.47 | 0.94 | 6 | 11 |
| Hexane | $\mathrm{C}_{6} \mathrm{H}_{14}$ | 1.92 | 86.175 | 436.90 | 913.47 | 1.65 | 8 | 18 |
| Heptane | $\mathrm{C}_{7} \mathrm{H}_{16}$ | 0.88 | 100.202 | 396.80 | 972.57 | 0.88 | 3 | 9 |
| Octane | $\mathrm{C}_{8} \mathrm{H}_{18}$ | 0.75 | 114.229 | 360.70 | 1,023.87 | 0.86 | 3 | 8 |
| Nonane | $\mathrm{C}_{9} \mathrm{H}_{20}$ | 0.00 | 128.255 | 330.70 | 1,070.47 | 0.00 | 0 | 0 |
| Decane | $\mathrm{C}_{10} \mathrm{H}_{22}$ | 0.00 | 142.282 | 304.60 | 1,111.87 | 0.00 | 0 | 0 |
| Air |  | 0.00 | 28.959 | 551.90 | 238.70 | 0.00 | 0 | 0 |
| Nitrogen | $\mathrm{N}_{2}$ | 2.44 | 28.014 | 492.50 | 227.14 | 0.68 | 12 | 6 |
| Oxygen | $\mathrm{O}_{2}$ | 0.00 | 31.999 | 731.40 | 278.24 | 0.00 | 0 | 0 |
| Carbon Dioxide | $\mathrm{CO}_{2}$ | 1.30 | 44.010 | 1,070.00 | 547.45 | 0.57 | 14 | 7 |
| Hydrogen Sulfide | $\mathrm{H}_{2} \mathrm{~S}$ | 0.00 | 34.082 | 1,306.50 | 672.48 | 0.00 | 0 | 0 |
| Hydrogen | $\mathrm{H}_{2}$ | 0.00 | 2.016 | 190.70 | 59.77 | 0.00 | 0 | 0 |
| Argon | Ar | 0.15 | 39.948 | 705.32 | 271.24 | 0.06 | 1 | 0 |
| Helium | He | 0.00 | 4.003 | 33.00 | 9.35 | 0.00 | 0 | 0 |
| Total |  | 100.00 |  |  |  | 24.08 | 649 | 411 |
| Sp. Gravity = |  | 0.832 |  |  |  |  |  |  |

For this sample, the gas sample molecular weight is 24.08 , the critical pressure is 649 psia , and the critical temperature is $411^{\circ} \mathrm{R}$. Now that the properties for the gas sample have been calculated, we can use these values to determine gas deviation factor and gas formation volume factor.

The specific gravity of gas is the weight of the gas relative to the weight of air. Once the molecular weight of the gas sample is known, we can simply divide it by the molecular weight of air to obtain its specific gravity. The specific gravity is calculated as follows.

$$
\text { Specific Gravity }=\frac{\text { Molecular Weight of Gas Sample }}{28.595}
$$

The Excel workbook that is part of the course material has a tab labeled "Gas Composition". The gas sample shown in Table 5 has been input into that spreadsheet. The area of the spreadsheet highlighted in yellow is available for input. The remainder of the spreadsheet is calculated.

## Determination of the Gas Deviation Factor

As mentioned in the previous sections, due to the molecular interactions of hydrocarbon molecules, hydrocarbon gases deviate from the ideal gas law. To account for this deviation, the gas deviation factor, z is used in the Ideal Gas Law. The relationship between pressure, volume, temperature and moles of gas then becomes:

$$
P V=n R T z
$$

where,
$P=$ pressure $($ psia - pounds per square inch absolute $)$
$V=$ volume $($ scf - standard cubic feet $)$
$T=$ temperature $\left({ }^{\circ} \mathrm{R}-\right.$ degrees Rankine $)$
$n=$ number of moles of gas (moles)
$R=$ ideal gas constant $\left(10.73\right.$ scf-psia/mole- $\left.{ }^{\circ} \mathrm{R}\right)$
$z=$ gas deviation factor

The determination of z is based on a chart created from the results of experiments with hydrocarbon gases and first published by Katz and Standing in 1942. A copy of the gas deviation factor chart is shown below.


The axes of the chart are Pseudoreduced Pressure ( Pr ) and Gas Deviation Factor (z). There are various lines on the chart for the Pseudoreduced Temperature (Tr). The term "pseudo" is used to denote that the values of Critical Pressure and Critical Temperature are derived from gas composition data, as shown in Table 5, for example. From here on we will use the terms Reduced Pressure and Reduced Temperature.

To use this chart to find z , we must first calculate the reduced pressure and temperature using the following equations:

$$
\begin{aligned}
& P_{r}=P / P_{c} \\
& T_{r}=T / T_{c}
\end{aligned}
$$

where,

$$
\begin{aligned}
& P_{r}=\text { reduced pressure } \\
& P=\text { measured pressure }(\mathrm{psia}) \\
& P_{c}=\text { critical pressure }(\mathrm{psia}) \\
& T_{r}=\text { reduced temperature } \\
& T=\text { measured temperature }\left({ }^{( } \mathrm{R}\right) \\
& T_{c}=\text { critical temperature }\left({ }^{\mathrm{R}}\right)
\end{aligned}
$$

The most efficient method to show how to determine the z , the gas deviation factor is to use an example.

## Example Problem:

A reservoir contains the gas whose composition is given in Table 5 . The reservoir pressure is 1,950 psia and the temperature is $106^{\circ} \mathrm{F}$. What is the gas deviation factor of the reservoir?

## Answer:

The reservoir temperature is given in ${ }^{\circ} \mathrm{F}$ and must be converted to ${ }^{\circ} \mathrm{R}$ as follows:

$$
T=460+106=566 \mathrm{R}
$$

From Table 5, the critical pressure is 649 psia and the critical temperature is $411{ }^{\circ} \mathrm{R}$.

The reduced pressure is:

$$
P_{r}=\frac{1950}{649}=3.00
$$

and the reduced temperature is:

$$
T_{r}=\frac{566}{411}=1.38
$$

Entering the chart as shown below with a reduced pressure of 3.00 and moving downward to an interpolated reduced temperature of 1.38 gives a gas deviation factor, z of 0.70 .


This method indeed works to determine the gas deviation factor. However, the method is time consuming and it is sometimes difficult to see details on the chart. Subsequent to the development of this chart, several digital calculation methods have been developed. The method created by Brill and Beggs in 1973 is accurate and only uses reduced pressure, reduced temperature, and gas gravity. A gas deviation factor calculator using this method is located in the Excel workbook under
the tab labeled " $\mathbf{z}$ Factor Calculator". The values for this example are entered into the worksheet. For the remainder of this course, we will be using the worksheet to determine gas deviation factors.

## Calculation of the Gas Formation Volume Factor

As gas is produced from a reservoir under pressure and temperature higher than those at the surface, gas expands. In layman's terms, a given number of molecules of gas take up less space in the reservoir than they do at the surface. To account for the change in gas volume from the surface to the reservoir, one uses the gas formation volume factor $\mathrm{B}_{\mathrm{g}}$.

The units for $\mathrm{Bg}_{\mathrm{g}}$ are reservoir cubic feet per standard cubic feet, of $\mathrm{ft}^{3} / \mathrm{scf}$. The gas formation volume factor is the number of cubic feet in the reservoir taken up by 1 standard cubic foot.

The denominator uses the units of "standard cubic feet". A standard cubic foot is defined by both a standard gas pressure and a standard gas temperature. In the United States, the standard temperature is $60^{\circ} \mathrm{F}\left(520^{\circ} \mathrm{R}\right)$. The standard pressure, however, changes with each state. For example, in Oklahoma, the standard pressure is 14.65 psia and in Louisiana it is 15.025 psia . A table of standard pressures for each state is provided in the Excel workbook under the tab "State Pressure Bases". For the purpose of this course, we will always use a pressure base of 14.65 psia unless otherwise stated.

The gas formation volume factor, $\mathrm{B}_{\mathrm{g}}$ as,

$$
B_{g}=\frac{P_{s c}}{T_{s c}} * \frac{z T}{P}
$$

where,

$$
\begin{aligned}
& \mathrm{T}_{\mathrm{sc}}=\text { standard temperature }\left({ }^{\circ} \mathrm{R}\right) \\
& \mathrm{P}_{\mathrm{sc}}=\text { standard pressure }(\mathrm{psia}) \\
& \mathrm{z}=\text { gas deviation factor } \\
& \mathrm{T}=\text { reservoir temperature }\left({ }^{\circ} \mathrm{R}\right) \\
& \mathrm{P}=\text { reservoir pressure }(\mathrm{psia})
\end{aligned}
$$

The gas deviation factor can be calculated using the spreadsheet labeled "z Factor Calculator" and is seen in column " $E$ " in the spreadsheet.

## Example Problem:

A reservoir contains the gas whose composition is given in Table 5. The reservoir pressure is 1,950 psia and the temperature is $106^{\circ} \mathrm{F}$. The standard pressure is 14.65 psia and standard temperature is $60^{\circ} \mathrm{F}\left(520^{\circ} \mathrm{R}\right)$. What is the gas formation volume factor?

## Answer:

The gas deviation factor can be found using the spreadsheet labeled "z Factor Calculator" and is equal to 0.705 .

The gas formation volume factor is:

$$
B_{g}=\frac{P_{s c}}{T_{s c}} * \frac{z T}{P}=\frac{14.65}{520} * \frac{(0.705) *(460+106)}{1,950}=0.0058 \mathrm{ft}^{3} / \mathrm{scf}
$$

Notice that in column "E" of the spreadsheet is the value of $\mathrm{B}_{\mathrm{g}}$.

## Discussion of Reservoir Area and Thickness

This course will not discuss how to determine the reservoir area or thickness. We will, however, discuss some of the methods used to obtain those values.

The area of the reservoir is defined as the areal extent of the reservoir known to contain gas. The thickness is defined as the vertical thickness of the reservoir containing gas. Multiplied together, the area times the thickness is the total rock volume of the reservoir. In the United States, areas are measured in acres and thickness in feet.

The reservoir area can be determined or estimated using information from wells drilled into the reservoir. The reservoir area can also be found using seismic methods. The data from either wells or seismic, or both, is mapped and the extent of the reservoir is found by extrapolating contours. The area of the reservoir can be determined using a planimeter or other method. Most 3-D geologic modeling software can calculate the area within given contour intervals.

The thickness of the reservoir can be determined in a similar manner to area, using well data and/or seismic data. The common method is to contour the thickness at each data point (either well or seismic) and overlay it on the reservoir contour map. To arrive at an average thickness, the area of each thickness interval is calculated and summed for the entire reservoir. The result of this is the rock volume of the reservoir, typically calculated as acre-feet. In the volumetric formula for OGIP,
these are the parameters A xh. If one desires to calculate the volume of the reservoir in cubic feet, use the following formula:

$$
V_{r}=43,560 * A * h
$$

where,
$\mathrm{V}_{\mathrm{r}}=$ reservoir volume in ft 3
$\mathrm{A}=$ reservoir area in acres
$\mathrm{H}=$ reservoir thickness in feet

Since reservoirs are usually quite large, it is more convenient to calculate the reservoir volume $\left(\mathrm{V}_{\mathrm{r}}\right)$ in millions of cubic feet as follows:

$$
V_{r}=0.04356 * A * h
$$

## Discussion of Porosity and Water Saturation

Porosity is defined as the portion of the reservoir void of rock expressed as a percentage of the rock volume. It is essentially the percentage of "holes" in the rock. If the porosity of a rock is $15 \%$, it means that $15 \%$ of the rock is void space and $85 \%$ of the rock is solid material. Porosity is the portion of the rock where all fluids exist. Porosity is given the symbol phi and can be in the units of decimal or percent.

Water saturation is the percentage of the pore space that is taken up by water. The remainder, or $100 \%$ less the water saturation, is the portion of the pore space that contains gas (typically referred to as hydrocarbon saturation). Water saturation, rather than hydrocarbon saturation has become a standard because it is typically derived from well logs which detect the presence of water, not hydrocarbons.

The most common method of obtaining porosity and water saturation is from well logs. Occasionally, cores are taken while drilling and sent to a lab where porosity and water saturations are determined. Well logs are obtained by running an electrical device on a cable to the bottom of a newly drilled well and pulling it up to the surface. During the pull to the surface, various rock properties are measured by the different types of devices connected to the cable. Typically measured are the natural radioactivity of the rock, the density of the rock, the electrical conductivity of the rock, hydrogen in the rock, travel of sound through the rock, etc. Based on these measurements, porosity and water saturation of the various rock layers can be calculated.

Both porosity and water saturations can vary throughout the thickness of the rock. They can also vary across the area of the reservoir. As such, the estimation of porosity and water saturation in a reservoir can be a very complicated process.

The most common way to account for the variations in porosity and water saturation is to create data points for each well of porosity times feet (porosity-feet) and porosity times feet times hydrocarbon saturation. These values are then contour mapped and the volumes measured and summarized. This results in the value of A xhx $\emptyset \mathrm{x}(1-\mathrm{Sw})$ in the volumetric equation. Table 6 below gives an example for a particular well of the calculation of porosity-feet and porosity x hydrocarbon-feet. The values are calculated as decimals, rather than percents.

| Table 6 <br> Calculation of Porosity-Feet and Water Saturation-Feet |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Depth <br> (ft) | h <br> (ft) | Porosity (\%) | $\begin{aligned} & \mathrm{S}_{\mathrm{w}} \\ & (\%) \\ & \hline \end{aligned}$ | $\begin{aligned} & \mathrm{S}_{\mathrm{hc}} \\ & (\%) \\ & \hline \end{aligned}$ | Porosity Feet |  Feet |
| 3614 | 2 | 20.5 | 19.9 | 80.1 | 0.410 | 0.328 |
| 3616 | 4 | 14.0 | 24.1 | 75.9 | 0.560 | 0.425 |
| 3620 | 6 | 11.4 | 25.3 | 74.7 | 0.684 | 0.511 |
| 3626 |  | 16.2 | 27.0 | 73.0 | 0.648 | 0.473 |
| 3630 | 2 | 17.9 | 26.7 | 73.3 | 0.358 | 0.262 |
| 3632 | 6 | 15.2 | 28.4 | 71.6 | 0.912 | 0.653 |
| 3638 | 5 | 13.8 | 26.7 | 73.3 | 0.690 | 0.506 |
| 3643 | 2 | 13.4 | 33.4 | 66.6 | 0.268 | 0.178 |
| 3645 | 3 | 12.8 | 36.8 | 63.2 | 0.384 | 0.243 |
| TOTAL | 34 |  |  |  | 4.914 | 3.580 |
| Notes: <br> $\mathrm{S}_{\mathrm{hc}}=$ Hydrocarbon saturation |  |  |  |  |  |  |
|  |  |  |  |  |  |  |

For this well, the average porosity and hydrocarbon saturation can be calculated as:

$$
\emptyset=\frac{\emptyset * h}{h}=\frac{4.914}{34}=0.144=14.4 \%
$$

In a similar fashion, the hydrocarbon saturation can be calculated by the following:

$$
S_{h c}=\frac{\emptyset * h * S_{h c}}{\emptyset * h}=\frac{3.580}{4.914}=0.729=72.9 \%
$$

Therefore, water saturation for this well is:

$$
S_{w}=100-S_{h c}=100-72.9=27.1 \%
$$

Notice that an arithmetic average of porosity that ignores the number of feet gives an incorrect value. Similarly, since water saturation and therefore hydrocarbon saturation are percentages of a given porosity, calculating the average value must take into account both the porosity and the number of feet of porosity. I will leave it to you to verify, but the arithmetic averages of porosity and water saturation from Table 6 are $15.0 \%$ and $27.6 \%$, respectively. Although the values appear to be fairly close to the weighted values (the correct ones) in this instance, they can be quite different in some cases.

## Calculation of Pore Volume, Hydrocarbon Pore Volume, and Water Volume

The pore volume of a reservoir is the total rock volume multiplied by the porosity as shown here:

$$
P V=0.04356 * A * h * \emptyset
$$

where,
$\mathrm{PV}=$ reservoir pore volume in MMcf
$\mathrm{A}=$ reservoir area in acres
$\mathrm{h}=$ reservoir thickness in feet
$\emptyset=$ reservoir porosity in decimal

The hydrocarbon pore volume is calculated as:

$$
H C P V=0.04356 * A * h * \emptyset *\left(1-S_{w}\right)
$$

where,
$\mathrm{HCPV}=$ hydrocarbon pore volume in MMcf
$\mathrm{A}=$ reservoir area in acres
$\mathrm{h}=$ reservoir thickness in feet
$\emptyset=$ reservoir porosity in decimal
$S_{w}=$ water saturation in decimal

The water volume in the reservoir expressed in millions of cubic feet is then obviously the difference between the two, or:

$$
P V-H C P V=0.04356 * A * h * \emptyset * S_{w}
$$

The HCPV is the reservoir volume available for gas in the reservoir. Since gas is measured and sold at standard conditions, it is necessary to convert the volume from reservoir conditions to surface conditions. This is done using the gas formation volume factor. When the gas formation volume factor at initial conditions is used, the subscript "i" is added. OGIP is calculated as follows:

$$
O G I P=\frac{0.04356 * A * h * \emptyset *\left(1-S_{w}\right)}{B_{g i}}
$$

where,
OGIP = original gas-in-place in MMscf (millions of standard cubic feet)
$\mathrm{A}=$ reservoir area in acres
$\mathrm{h}=$ reservoir thickness in feet
$\emptyset=$ reservoir porosity in decimal
$\mathrm{S}_{\mathrm{w}}=$ water saturation in decimal
$\mathrm{B}_{\mathrm{gi}}=$ initial gas formation volume factor in $\mathrm{ft}^{3} / \mathrm{scf}$

## Calculation of Residual Gas Volume

Residual gas is the gas remaining in the reservoir at abandonment. If one calculates the original gas-in-place and has the cumulative gas production information, the residual gas is simply the difference between the two as:

$$
G_{r e s}=O G I P-G
$$

where,
$\mathrm{G}_{\text {res }}=$ residual gas in MMscf
OGIP = OGIP = original gas-in-place in MMscf
$\mathrm{G}=$ cumulative gas production in MMscf

We will term the volume in the reservoir taken up by the residual gas as $\mathrm{HCPV}_{\text {res. }}$. As $\mathrm{CO}_{2}$ is injected and the reservoir pressure reaches the sequestration pressure (initial reservoir pressure), this is the amount of reservoir volume that will contain the residual gas. The $\mathrm{HCPV}_{\text {res }}$ is calculated as:

$$
H C P V_{\text {res }}=G_{\text {res }} * B_{g i}
$$

where,
$\mathrm{HCPV}_{\text {res }}=$ residual hydrocarbon pore volume in MMcf

## Example Problem:

A reservoir contains the gas whose composition is given in Table 5. The average reservoir depth is 4,500 feet. The reservoir covers an area of 2,860 acres at a thickness of 28 feet. The porosity of the reservoir is $18.6 \%$ and the average water saturation is $32 \%$. The reservoir pressure is 1,950 psia and the temperature is $106^{\circ} \mathrm{F}$. The standard conditions are 14.65 psia and $60{ }^{\circ} \mathrm{F}$. The cumulative production is $71,048 \mathrm{MMscf}$.
a) What is the hydrocarbon pore volume?
b) What is the water volume?
c) What is the OGIP?
d) What is the residual gas volume at standard conditions in MMscf?
e) What is the residual hydrocarbon pore volume in the reservoir?

Feel free to use the worksheet to perform the calculations.

## Answer:

a) From prior calculations and determinations from the examples above, we already know the following:

$$
\begin{aligned}
& \mathrm{z}=0.705 \\
& \mathrm{~B}_{\mathrm{g}}=0.0058 \mathrm{ft}^{3} / \mathrm{scf}
\end{aligned}
$$

$$
H C P V=0.04356 * A * h * \emptyset=0.04356 * 2860 * 28 * .186=648.8 M M c f
$$

b) The water volume is:

$$
\begin{aligned}
\text { Water Volume } & =0.04356 * A * h * \emptyset * S_{w}=0.04356 * 2860 * 28 * .186 * 0.32 \\
= & 207.6 \text { MMcf }
\end{aligned}
$$

c) From prior calculations and determinations from examples above, we already know the following:

$$
\begin{aligned}
& \mathrm{z}=0.705 \\
& \mathrm{~B}_{\mathrm{gi}}=0.0058 \mathrm{ft}^{3} / \mathrm{scf}
\end{aligned}
$$

The OGIP is:

$$
\begin{gathered}
\text { OGIP }=\frac{0.04356 * A * h * \emptyset *\left(1-S_{w}\right)}{B_{g i}}=\frac{0.04356 * 2860 * 28 * .186 *(1-.32)}{0.0058} \\
=76,068 \mathrm{MMsc} f
\end{gathered}
$$

d) The residual gas volume is calculated as:

$$
G_{r e s}=O G I P-G=76,068-71,048=5,020 M M s c f
$$

e) The residual hydrocarbon pore volume in the reservoir is:

$$
H C P V_{\text {res }}=G_{\text {res }} * B_{g i}=5,020 * .0058=29 M M c f
$$

## $\mathrm{CO}_{2}$ Sequestration in Abandoned Gas Reservoirs

The estimation of the amount of $\mathrm{CO}_{2}$ that can be sequestered in abandoned gas reservoirs is a bit more complicated than that of an aquifer. The reason is because we have both water-filled porosity and gas-filled porosity in the reservoir. At abandonment, the gas in the reservoir has expanded to fill all the pore space in the reservoir that is not filled by water. This is known as the hydrocarbon pore volume (HCPV). When $\mathrm{CO}_{2}$ is injected into the reservoir and pressure increases, this remaining gas (termed residual gas) will be compressed and take up some of the HCPV. Because of this, a portion of the HCPV will not be available for $\mathrm{CO}_{2}$ sequestration.

The diagrams below show the fluid distributions in an abandoned gas reservoir before and after $\mathrm{CO}_{2}$ sequestration.


As can be seen, $\mathrm{CO}_{2}$ will be sequestered in both the hydrocarbon pore space and dissolved in reservoir water. It is assumed that the sequestration pressure will be equal to the initial reservoir pressure.

The estimation of $\mathrm{CO}_{2}$ sequestration in abandoned gas reservoirs involves several steps. The assumption for this method is that there is sufficient information available for the calculations. The following data are needed for these calculations:

- Reservoir area
- Reservoir height
- Average porosity
- Average water saturation
- Gas composition or gas gravity and critical pressure and temperature
- Initial reservoir pressure
- Reservoir temperature
- Cumulative gas production

An additional assumption is that the $\mathrm{CO}_{2}$ sequestration pressure will be equal to the original reservoir pressure.

The estimation of $\mathrm{CO}_{2}$ sequestration in abandoned gas reservoirs involves the following steps:

1) Obtain the data listed above
2) Calculate the hydrocarbon pore volume (HCPV) and the water volume in the reservoir
3) Calculate the gas formation volume factor $\left(\mathrm{B}_{\mathrm{g}}\right)$ at the initial reservoir pressure
4) Calculate the residual gas volume at standard conditions and at $\mathrm{CO}_{2}$ sequestration pressure (the initial reservoir pressure)
5) Calculate the HCPV available for $\mathrm{CO}_{2}$ sequestration
6) Using the NIST website, find the $\mathrm{CO}_{2}$ density at the $\mathrm{CO}_{2}$ sequestration pressure and reservoir temperature
7) Calculate the lb of $\mathrm{CO}_{2}$ that can be sequestered in the HCPV
8) Determine $\mathrm{CO}_{2}$ solubility at the $\mathrm{CO}_{2}$ sequestration pressure
9) Calculate the lb of $\mathrm{CO}_{2}$ that can be sequestered in the reservoir water
10) Sum the lb of $\mathrm{CO}_{2}$ sequestered in the HCPV and the reservoir water
11) Calculate at standard conditions the total $\mathrm{CO}_{2}$ that can be sequestered in the reservoir

To show each of these steps, we will use an example. The reservoir chosen will be identical to the example used for the aquifer, except the water saturation in this example will be $32 \%$ (not $100 \%$ as in the aquifer example). By using the same example reservoir, one will be able to compare the amount of $\mathrm{CO}_{2}$ sequestered in an aquifer with the amount sequestered in an abandoned gas reservoir.

This example problem is solved in the spreadsheet in the Excel workbook titled "Sequestration Gas Res" on row 4.

## Example Problem:

Estimate how much $\mathrm{CO}_{2}$ can be sequestered in an abandoned gas reservoir with the following properties. Express the answer in both pounds of $\mathrm{CO}_{2}$ and standard cubic feet of $\mathrm{CO}_{2}$ that can be sequestered.

Reservoir depth $=5,400 \mathrm{ft} \quad$ Reservoir area $=3,200$ acres $\quad$ Reservoir height $=50 \mathrm{ft}$
Reservoir porosity $=24.1 \% \quad$ Reservoir temp $=118^{\circ} \mathrm{F} \quad$ Reservoir pressure $=2,350 \mathrm{psia}$
Reservoir water saturation $=32 \% \quad$ Cumulative Gas $=204,420$ MMscf
Critical Pressure $=649$ psia Critical Temperature $=411^{\circ} \mathrm{R}$
Standard pressure $=14.65 \mathrm{psia} \quad$ Standard temp $=60^{\circ} \mathrm{F}$

## Answer:

Step 1) This is just the given data.

Step 2) The hydrocarbon pore volume is given by:

$$
\begin{gathered}
H C P V=0.04356 * A * h * \emptyset *\left(1-S_{w}\right)=0.04356 * 3200 * 50 * .241 *(1-.32) \\
=1,142.2 \text { MMcf }
\end{gathered}
$$

The water volume is given by:

$$
\begin{aligned}
\text { Water Volume } & =0.04356 * A * h * \emptyset * S_{w}=0.04356 * 3200 * 50 * .241 * 0.32 \\
= & 537.5 M M c f
\end{aligned}
$$

Step 3) The gas deviation factor must first be determined to use in the calculation of Bg. The reduced pressure and temperature are:

$$
\begin{gathered}
P_{r}=\frac{2350}{649}=3.62 \\
T_{r}=\frac{(460+118)}{411}=1.41
\end{gathered}
$$

The gas deviation factor, z , from the " z Factor Calculator" worksheet is 0.718 .

The gas formation volume factor, Bg , is calculated as:

$$
B_{g}=\frac{P_{s c}}{T_{s c}} * \frac{z T}{P}=\frac{14.65}{520} * \frac{(0.718) *(460+118)}{2,350}=0.0050 \mathrm{ft}^{3} / \mathrm{scf}
$$

Step 4) The residual hydrocarbon volume at standard conditions is the OGIP minus the cumulative gas production. The OGIP is calculated as:

$$
\begin{gathered}
\text { OGIP }=\frac{0.04356 * A * h * \emptyset *\left(1-S_{w}\right)}{B_{g i}}=\frac{0.04356 * 3200 * 50 * .241 *(1-.32)}{0.0050} \\
=228,436 \mathrm{MMscf}
\end{gathered}
$$

The residual gas is then determined by:

$$
G_{r e s}=O G I P-G=228,436-204,420=24,016 M M s c f
$$

The reservoir volume at sequestration pressure taken up by the residual gas is:

$$
H C P V_{\text {res }}=G_{\text {res }} * B_{g}=24,016 * 0.0050=120.1 M M c f
$$

Step 5) The hydrocarbon pore volume available for sequestration is:

$$
H C P V_{\text {seq }}=H C P V-H C P V_{\text {res }}=1,142.2-120.1=1,022.1 \mathrm{MMcf}
$$

Another way to solve for this is to assume (correctly) that the volume available is the cumulative gas volume at original reservoir conditions. This is indeed equal to the available sequestration volume as calculated below:

$$
H C P V_{\text {seq }}=G * B_{g}=204,420 * 0.0050=1,022.1 \mathrm{MMcf}
$$

Step 6) Using the NIST website link given below, the density of $\mathrm{CO}_{2}$ at a pressure of $2,350 \mathrm{psia}$ and a temperature of 1180 F is $46.385 \mathrm{lb} / \mathrm{ft}_{3}$.

## Thermophysical Properties of Fluid Systems (nist.gov)

Step 7) From Step 5 above, the available sequestration volume in the reservoir is $1,022.1$ MMcf. The amount of $\mathrm{CO}_{2}$ that can be stored is:

$$
\mathrm{CO}_{2} \text { Sequestered in } \mathrm{HCPV}=H C P V_{\text {seq }} * \rho_{\mathrm{CO} 2}=1,022.1 * 46.385=47,410 \text { million lb CO}
$$

Step 8) To use the chart, the temperature and pressure must be converted to ${ }^{\circ} \mathrm{C}$ and bars, respectively as shown below:

$$
\begin{gathered}
T_{o C}=\frac{\left(T_{o F}-32\right)}{1.8}=\frac{(118-32)}{1.8}=48 C \\
P_{b a r}=\frac{P_{p s i a}}{14.504}=\frac{2,350}{14.696}=160 \mathrm{~atm}
\end{gathered}
$$



The solubility is $5.7 \mathrm{lb} \mathrm{CO}_{2} / 100 \mathrm{lb}_{2} \mathrm{O}$.

Step 9) The weight of water in pounds is simply the volume multiplied by the water density of $62.4 \mathrm{lb} / \mathrm{ft}^{3}$ as follows:

$$
W=P V * \rho_{w}=537.5 * 62.4=33,540 \text { million lb of water }
$$

The volume of $\mathrm{CO}_{2}$ that can be sequestered in reservoir water is:
Sequestered $\mathrm{CO}_{2}=$ Water Mass $x \mathrm{CO}_{2}$ Solubility $=33,540 * \frac{5.7}{100}=1,912$ million $\mathrm{lb} \mathrm{CO}_{2}$

Step 10) The total amount of $\mathrm{CO}_{2}$ that can be sequestered in the reservoir is the sum of the amount sequestered in the pore volume and dissolved in the reservoir water as follows:

$$
\text { Total } \mathrm{CO}_{2} \text { Sequestered }=47,410+1,912=49,322 \text { million lb } \mathrm{CO}_{2}
$$

Step 11) The amount of $\mathrm{CO}_{2}$ at standard conditions that can be sequestered is:

$$
\begin{gathered}
\text { Sequestered } \mathrm{CO}_{2} \text { at Std Conditions }=\frac{\text { Sequestered } \mathrm{CO}_{2} \text { in } \mathrm{lbs}}{\rho C O 2_{\text {std }}}=\frac{49,322}{0.115} \\
=428,887 \mathrm{MMscf}
\end{gathered}
$$

There has been much talk about sequestering $\mathrm{CO}_{2}$ in aquifers. However, as seen from the calculations above, much more $\mathrm{CO}_{2}$ can be sequestered in abandoned gas reservoirs. Of the $\mathrm{CO}_{2}$ sequestered in the above example, the amount sequestered in the HCPV as a percentage of the total sequestered is:

$$
\text { Percent Sequestered in Pore Space }=100 * \frac{47,410}{49,322}=96 \%
$$

So, in this example, even with a water saturation of $32 \%$ (about a third of the porosity), the amount of $\mathrm{CO}_{2}$ sequestered in the reservoir is less than $5 \%$ of the total.

When we compare the amount of $\mathrm{CO}_{2}$ sequestered in this example of an abandoned gas reservoir to that of an aquifer of the same size and pore volume (original example) we see it is much larger. Using $\mathrm{CO}_{2}$ sequestered at standard conditions for comparison, the ratio of $\mathrm{CO}_{2}$ sequestered in the abandoned gas reservoir to aquifer is:

$$
\text { Ratio Gas Reservoir to Acquifer }=\frac{428,887}{51,948}=8.3
$$

So, there is over 8 times more $\mathrm{CO}_{2}$ sequestered in the abandoned gas reservoir as aquifer.

## $\mathrm{CO}_{2}$ Sequestration in Abandoned Gas Reservoirs - Limited Information

The previous section gives detailed instructions on calculating $\mathrm{CO}_{2}$ sequestration volumes when significant reservoir information is available. This may be the case when a particular reservoir is being offered by the operator for $\mathrm{CO}_{2}$ sequestration or personnel at the operating company are evaluating the reservoir internally for use as storage. However, if one is using public data, limited information may only be available for a cursory evaluation.

The method outlined here enables one to estimate the amount of $\mathrm{CO}_{2}$ that may be sequestered in the pore space of an abandoned gas reservoir. Since water saturation will not be considered (it is usually not available as part of the limited information), only the amount of $\mathrm{CO}_{2}$ sequestered in the pore space can be calculated. However, as shown in previous examples, the amount that could be sequestered in the reservoir water is likely small and on the order of $5 \%$ or less of the total sequestered $\mathrm{CO}_{2}$.

In some cases, reservoir information may be available from state agencies (i.e., oil and gas commissions) or geologic society publications. Some state agencies keep very good field records while others only collect basic information.

The mere basic information needed to estimate $\mathrm{CO}_{2}$ sequestration volumes is:

- Initial reservoir pressure
- Reservoir temperature
- Cumulative gas production
- Gas analysis or at least the gas gravity

Probably the most difficult item to find on the above list is the gas composition or gas gravity. If gas analysis or gas gravity is not available, there are some resources available in the public domain. The US Bureau of Mines (no longer in existence) used to maintain books that contained reported gas analyses on wells whose gas was analyzed. A book containing gas analyses for the years 19171958 titled Analysis of Natural Gases 1917-1985 can be found in pdf format from the National Technical Reports Library (US Department of Commerce) at this internet address:

## Analyses of Natural Gases, 1917-85.| National Technical Reports Library - NTIS

A good deal of this information is in digital form and can be found as a downloadable .csv file. Once imported into Excel, filters can be set up to hopefully find a gas analysis in or near the field and in the reservoir of study. That file can be downloaded from the US Geological Survey at this site:

Natural Gas Compositional Analyses Dataset of Gases from United States Wells - ScienceBaseCatalog
The data from these sources can be easily input into the "Gas Composition" worksheet to find the critical pressure and temperature needed to determine the gas deviation factor.

In cases where only the gas gravity is known, there are some correlations that enable one to find the associated critical temperature and pressure. A table of gas gravity versus critical pressure and critical temperature was prepared by the California Natural Gasoline Association in 1941. This table can be found in several publications and is still a good source of data.

A table of the data has been placed in the Excel workbook under the tab " Sp Gr vs Pc Tc ".

| Gas Specific Gravity vs $\mathrm{P}_{\mathrm{c}}$ and $\mathrm{T}_{\mathrm{c}}$ |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Sp. Gr. | $\begin{gathered} P_{c} \\ \text { (psia) } \end{gathered}$ | $\begin{gathered} \mathrm{T}_{\mathrm{c}} \\ \left({ }^{\circ} \mathrm{R}\right) \\ \hline \end{gathered}$ | Sp. Gr. | $\begin{gathered} \mathbf{P}_{\mathrm{c}} \\ (\text { psia }) \end{gathered}$ | $\mathrm{T}_{\mathrm{c}}$ <br> ( ${ }^{\circ} \mathrm{R}$ ) | Sp. Gr. | $\begin{gathered} \mathbf{P}_{\mathrm{c}} \\ \text { (psia) } \end{gathered}$ | $\begin{gathered} \mathrm{T}_{\mathrm{c}} \\ \left({ }^{\circ} \mathrm{R}\right) \\ \hline \end{gathered}$ |
| 0.55 | 673 | 336 | 0.75 | 667 | 408 | 0.95 | 660 | 474 |
| 0.56 | 673 | 341 | 0.76 | 667 | 411 | 0.96 | 660 | 477 |
| 0.57 | 672 | 346 | 0.77 | 666 | 415 | 0.97 | 659 | 481 |
| 0.58 | 672 | 350 | 0.78 | 666 | 418 | 0.98 | 659 | 484 |
| 0.59 | 672 | 354 | 0.79 | 666 | 421 | 0.99 | 659 | 487 |
| 0.60 | 671 | 358 | 0.80 | 665 | 424 | 1.00 | 658 | 491 |
| 0.61 | 671 | 362 | 0.81 | 665 | 428 | 1.01 | 658 | 494 |
| 0.62 | 671 | 365 | 0.82 | 665 | 431 | 1.02 | 657 | 497 |
| 0.63 | 670 | 368 | 0.83 | 665 | 434 | 1.03 | 656 | 500 |
| 0.64 | 670 | 372 | 0.84 | 664 | 438 | 1.04 | 656 | 504 |
| 0.65 | 670 | 375 | 0.85 | 664 | 441 | 1.05 | 655 | 507 |
| 0.66 | 670 | 378 | 0.86 | 664 | 444 | 1.06 | 655 | 510 |
| 0.67 | 669 | 382 | 0.87 | 663 | 448 | 1.07 | 654 | 514 |
| 0.68 | 669 | 385 | 0.88 | 663 | 451 | 1.08 | 654 | 517 |
| 0.69 | 669 | 388 | 0.89 | 662 | 454 | 1.09 | 653 | 520 |
| 0.70 | 668 | 392 | 0.90 | 662 | 457 | 1.10 | 652 | 524 |
| 0.71 | 668 | 395 | 0.91 | 662 | 461 | 1.11 | 652 | 527 |
| 0.72 | 668 | 398 | 0.92 | 662 | 464 | 1.12 | 651 | 530 |
| 0.73 | 668 | 401 | 0.93 | 661 | 467 | 1.13 | 651 | 534 |
| 0.74 | 667 | 405 | 0.94 | 661 | 471 | 1.14 | 650 | 537 |

To use the table, simply start with the gas gravity and look to the right to find the critical pressure and temperature. Now one can find the gas deviation factor and with the reservoir pressure and temperature, the gas formation volume factor from the spreadsheet " $z$ Factor Calculator".

The following steps should be followed to estimate $\mathrm{CO}_{2}$ sequestration in an abandoned gas reservoir with limited information:

1) Obtain reservoir pressure, temperature, cumulative gas production, and gas gravity or gas composition
2) Calculate the gas formation volume factor
3) Calculate the available pore volume for $\mathrm{CO}_{2}$ using cumulative gas production
4) Calculate the $\mathrm{CO}_{2}$ density at initial reservoir pressure
5) Calculate the lb of $\mathrm{CO}_{2}$ that can be sequestered in the reservoir
6) Calculate the amount of $\mathrm{CO}_{2}$ at standard conditions that can be sequestered

All of the above can be done using the spreadsheet under the tab "Seq Limited Info".

We will now follow an example using the same reservoir as the last two examples. We should find that we are able to store the same amount of $\mathrm{CO}_{2}$ in the pore space as the last example.

## Example Problem:

Estimate how much $\mathrm{CO}_{2}$ can be sequestered in an abandoned gas reservoir with the following properties. Express the answer in both pounds of $\mathrm{CO}_{2}$ and standard cubic feet of $\mathrm{CO}_{2}$ that can be sequestered.

Reservoir depth $=5,400 \mathrm{ft} \quad$ Reservoir temp $=118^{\circ} \mathrm{F} \quad$ Reservoir pressure $=2,350 \mathrm{psia}$
Cumulative Gas $=204,420 \mathrm{MMscf}$
Critical Pressure $=649$ psia Critical Temperature $=411^{\circ} \mathrm{R}$
Standard pressure $=14.65 \mathrm{psia} \quad$ Standard temp $=60^{\circ} \mathrm{F}$

## Answer:

Step 1) This is the given data.
Step 2) The gas deviation factor must first be determined to use in the calculation of Bg. The reduced pressure and temperature are:

$$
\begin{gathered}
P_{r}=\frac{2350}{649}=3.62 \\
T_{r}=\frac{(460+118)}{411}=1.41
\end{gathered}
$$

The gas deviation factor, $z$, from the " $z$ Factor Calculator" worksheet is 0.718 .

The gas formation volume factor, Bg , is calculated as:

$$
B_{g}=\frac{P_{s c}}{T_{s c}} * \frac{z T}{P}=\frac{14.65}{520} * \frac{(0.718) *(460+118)}{2,350}=0.0050 \mathrm{ft}^{3} / \mathrm{scf}
$$

Step 3) The volume available is the cumulative gas volume at original reservoir conditions. This is calculated below:

$$
H C P V_{\text {seq }}=G * B_{g}=204,420 * 0.0050=1,022 M M c f
$$

Step 4) Using the NIST website link given below, the density of $\mathrm{CO}_{2}$ at a pressure of $2,350 \mathrm{psia}$ and a temperature of $118^{\circ} \mathrm{F}$ is $46.385 \mathrm{lb} / \mathrm{ft}_{3}$.

## Thermophysical Properties of Fluid Systems (nist.gov)

Step 5) From Step 3 above, the available sequestration volume in the reservoir is 1,022 MMcf. The amount of $\mathrm{CO}_{2}$ that can be stored is:

$$
\mathrm{CO}_{2} \text { Sequestered in } \mathrm{HCPV}=H C P V_{\text {seq }} * \rho_{C O 2}=1,022 * 46.385=47,405 \text { million lb CO }{ }_{2}
$$

Step 6) The amount of $\mathrm{CO}_{2}$ at standard conditions that can be sequestered is:

$$
\begin{gathered}
\text { Sequestered } \mathrm{CO}_{2} \text { at Std Conditions }=\frac{\text { Sequestered } \mathrm{CO}_{2} \text { in lbs }}{\rho C O 2_{\text {std }}}=\frac{47,405}{0.115} \\
=412,217 \mathrm{MMscf}
\end{gathered}
$$

In comparing the $\mathrm{CO}_{2}$ sequestered of 17,410 million ${\mathrm{lb} \mathrm{CO}_{2}}$ with Step 7 of the previous example, they are indeed the same value.

This example is found on the spreadsheet "Seq Limited Info" on row 4.

As seen, this method is an excellent way to review a large volume of reservoirs using very few steps.

## Conclusion

Hopefully, after taking this course you will feel confident to screen potential reservoirs by sequestration volume. When undertaking a $\mathrm{CO}_{2}$ sequestration project, estimating the sequestration volume of a potential reservoir is likely the most important consideration. This is especially true when the volume from the $\mathrm{CO}_{2}$ source requiring sequestration is known.

It is important to estimate $\mathrm{CO}_{2}$ sequestration for several reservoirs as other considerations can affect the determination of the final selection for sequestration. Knowing the reservoir volume is sufficient for sequestration will eliminate that as a concern for project success.

Although it wasn't covered in this course, one must keep in mind other factors that can eliminate a reservoir as a sequestration candidate. These include:

- Lack of access to the reservoir
- Inability to purchase or obtain rights to the reservoir
- High injection rates
- Proximity to the source of $\mathrm{CO}_{2}$
- Economics of the project

Some of the above items may be discovered during the sequestration volume estimation process (i.e., lack of access), while others may not be known until later in the planning stage (economics of the project). The estimation of sequestration volumes can be performed regardless of what stage of planning one is in.

## References

1. Amyx, James W., Bass, Daniel M. Jr., Whiting, Robert L., 1960, Petroleum Reservoir Engineering - Physical Properties, McGraw-Hill Book Company, pp. 211-447.
2. Beggs, H. Dale, 1984, Gas Production Operations, OGCI Publications, pp. 15-48.
3. Brill J. and Beggs H, 1973, A Study of Two-Phase Flow in Inclined Pipes, The University of Tulsa.
4. Campbell, John M., 1974, Gas Conditioning and Processing, Campbell Petroleum Series, pp. 1-37.
5. Clark, Norman J., 1969, Elements of Petroleum Reservoirs, Society of Petroleum Engineers, pp. 31-55.
6. Craft, B. C., Hawkins, M. F., 1959, Applied Petroleum Reservoir Engineering, Prentice-Hall, Inc., pp. 1-87.
7. Gas Processors Suppliers Association, 2004, Engineering Data Book, Gas Processors Suppliers Association, Section 23.
8. Interstate Oil and Gas Compact Commission, 2000, Back-Pressure Testing of Gas Wells, IOGCC, pg. 128-129.
9. Katz, Donald L, etal, 1959, Handbook of Natural Gas Engineering, McGraw-Hill Book Company, pp. 69-188.
10. McCain, William D. Jr., 1973, The Properties of Petroleum Fluids, Petroleum Publishing Company, pp. 3-42, 44-81, 82-139.
11. Mungan, N, 1981, Improved Oil Recovery, Interstate Oil Compact Commission, pp. 113-172.
12. National Institute of Standards and Technology, 2021, NIST Chemistry WebBook, SRD 69, U.S. Department of Commerce, https://webbook.nist.gov/chemistry/fluid/.
13. Standing, M. B., 1977, Volumetric and Phase Behavior of Oil Field Hydrocarbon Systems, Society of Petroleum Engineers of AIME, pp. 20-32.
